

# Density of Methanol + Water between 250 K and 440 K and up to 40 MPa and Vapor–Liquid Equilibria from 363 K to 440 K

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The density of methanol + water has been measured between 257.3 K and 442.15 K as a function of pressure at five compositions by means of a high-pressure apparatus implementing a metal bellows as a simple cell. Bubble pressures have been determined at five temperatures between 363.15 K and 442.15 K. They are compared with literature data that have been correlated by using the “excess function-equation of state” model.

## Introduction

A knowledge of the thermodynamic properties of the methanol + water system is very important in order to improve the prediction of phase equilibria. Numerous vapor-liquid equilibria, excess enthalpies, and excess volumes at atmospheric pressure have been measured at temperatures between 298.15 K and 333.15 K (McGlashan and Williamson, 1976; Benson and Kiyohara, 1980; Patel and Sandler, 1985). Few data exist above these temperatures and under pressure. Excess volumes have been reported by Eastal and Woolf (1985) between 278 K to 323 K at pressures to 280 MPa and recently by Xiao et al. (1997) between 323 K and 573 K at two pressures of 7 MPa and 13.5 MPa. On the other hand, vapor–liquid equilibria have been measured by Griswold and Wong (1952) at four temperatures between 373 K and 523 K, by Schroder (1958) at 413.15 K, and by Hirata and Suda (1967) and Hirata et al. (1975) at pressures of 0.3 MPa and 0.5 MPa.

In this work, densities are reported as a function of pressure for methanol + water over a wide range of temperature and composition. We have also determined bubble pressures at five temperatures between 373 K and 423 K.

## Experimental Section

**Materials.** Methanol provided by Prolabo (Paris, France) had a stated minimum purity of 99%. It was purified by fractional distillation on a 60-plate Oldershaw type column and was controlled by gas-chromatographic analysis (purity > 99.90%). The main impurity was water (<0.10%). Water used was distilled twice.

**Apparatus and Procedure.** A schematic diagram of the apparatus is shown in Figure 1, and a more detailed description is given elsewhere (Hocq, 1994; Hocq et al., 1995).

The apparatus consists mainly of an equilibrium cell that includes a bellows and two sapphire windows for visual observation, a constant-temperature air bath, a high-pressure recirculation pump, a micrometric table, pressure

and temperature transducers, and regulation and vacuum systems. Figure 2 shows a cross-sectional view of the metal bellows whose length varies from 8 cm to 32 cm.

Pressure is measured by using five Schenk extensiometric gauge pressure transducers (type P3MA) and controlled by a digital Heise gauge (model 901B) calibrated to NIST standards before use. The pressure measurements were estimated to be accurate to within  $\pm 0.01$  MPa.

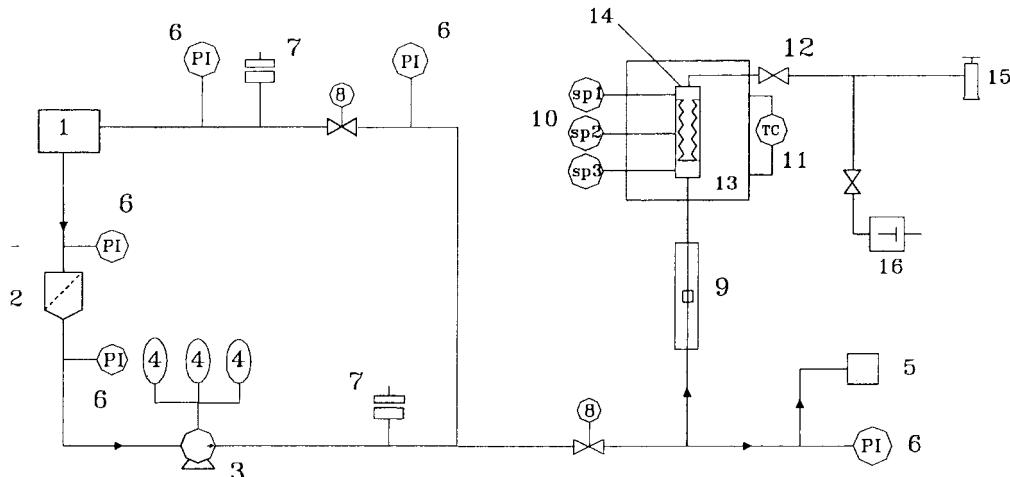
The temperature of the air bath is kept constant with an uncertainty of  $\pm 0.05$  K by an electronic controller. The temperature was determined with three platinum resistance thermometers inserted into the cell with an estimated accuracy of  $\pm 0.05$  K.

The displacement bellows is detected by a magnetic core whose position is measured by means of a micrometric table. The bellows was calibrated by measuring the *PVT* properties of toluene and methanol at various temperatures between 240 K and 450 K in the range of pressures from 0.4 MPa to 64 MPa covering the bellows displacement from 8 cm to 32 cm, which corresponds to the volume variation from 30 cm<sup>3</sup> to 150 cm<sup>3</sup>. Densities of methanol and toluene were calculated with the Goodwin (1987, 1989) equations of state. A calibration equation, established between the volume and the number of micrometric steps, reproduces data within 0.2%.

The first step in the experimental procedure is to introduce into the filling cell a known amount of the first component using a syringe. After degassing, the sample is transferred from the filling into the bellows by distillation using liquified nitrogen. The filling cell is weighed before and after sample transfer. The mass measurements were reproducible to within 0.0001 g. The second component was added using the same technique.

The rest of the operation was managed by a computer. It consisted of adjusting the working temperature and increasing the pressure up to 70 MPa, the micrometric table being initialized by moving to its mechanical zero. When the equilibrium state is reached in about 20 min, temperature, pressure, and bellows position were recorded. The volume of the mixture was calculated with the calibration equation. In the single-phase region, the measurements were carried out in intervals of pressure of 1.5 MPa for the given temperature. In the two-phase region, these

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**Figure 1.** Schematic diagram of the experimental apparatus: (1) oil tank; (2) filter; (3) piston pump; (4) shock absorber; (5) pressure gauge "Heise"; (6) pressure gauges; (7) regulation valves; (9) micrometric table; (10) platinum resistance thermometer; (11) thermic regulation; (12) product introduction valve; (13) climatic fence; (14) autoclave and bellows; (15) filling cell; (16) vacuum pump.

are carried out at given intervals of density in adjusting the number of micrometric steps. The experiment continues by decompressing the cell to the next pressure by opening and closing regulation valves (8). A measurement for a single isotherm took 1 day.

### Experimental Results

Table 1 lists the density and pressure measurements of methanol (1) + water (2) for five compositions at nine temperatures ranging from 257.3 K to 442.15 K. For the mole fractions of methanol of 0.1061 and 0.2872, the *PVT* properties have not been measured along the isotherm of 257 K on account of the vicinity of melting points of methanol + water.

In Figure 3, the volume is plotted as a function of pressure at constant composition ( $x_1 = 0.4980$ ). The bubble pressure corresponds to the intersection of the curves representing the one-phase and two-phase regions. The bubble pressure and composition data at five temperatures (from 363.15 K to 442.15 K) are presented in Table 2. We have not reported bubble pressures at lower temperatures since the values are too small.

### Results and Discussion

It was difficult to compare directly our  $P, \rho, T$  data with those reported in the literature since they are few in number and are often outside the temperatures and pressures studied. Recently, Xiao et al. (1997) developed a modified corresponding-states model based on their measurements and available at temperatures between 323 K and 573 K and pressures between 7 MPa and 13.5 MPa. To evaluate our data, this model was used. The mean relative deviation and the mean relative bias between experimental and calculated densities defined by

$$\Delta\rho/\rho(\%) = \frac{100}{N} \sum_{i=1}^N \left| \frac{\rho_{\text{exp},i} - \rho_{\text{cal},i}}{\rho_{\text{exp},i}} \right| \quad (1)$$

$$\beta_r(\rho) = \frac{100}{N} \sum_{i=1}^N \frac{\rho_{\text{exp},i} - \rho_{\text{cal},i}}{\rho_{\text{exp},i}} \quad (2)$$

are presented in Table 3. Agreement seems quite acceptable.

For vapor-liquid equilibria, the methanol + water data were correlated using the model "excess function-equation of state" described previously (Pénéroux et al., 1989). To

represent the properties of pure compounds a volume-translated Peng-Robinson equation of state was adopted:

$$P = \frac{RT}{\tilde{v} - b} - \frac{a(T)}{\tilde{v}(\tilde{v} + \gamma b)} \quad \text{with } \gamma = 2(\sqrt{2} + 1) \quad (3)$$

The pseudo-covolume  $\tilde{b}$  was calculated from critical constants, and the dependent-temperature function  $a(T)$  is given by

$$a(T) = a(T_b) \left\{ 1 + m_1 \left[ 1 - \left( \frac{T}{T_b} \right)^{0.05} \right] - m_2 \left( 1 - \frac{T}{T_b} \right) \right\} \quad (4)$$

where  $a(T_b)$  is the value of parameter  $a$  at the normal boiling temperature  $T_b$ . Parameters  $m_1$  and  $m_2$  were adjusted in accordance with vapor pressures of pure components. Their values are listed in Table 4.

The excess function is defined at packing fraction ( $\eta = \tilde{b}/\tilde{v}$ ), and the mixture equation has the following form

$$z = \frac{1}{1 - \eta} - \sum_{i=1}^p \frac{x_i a_i}{RT b_i} Q'(\eta) + \frac{1}{2} \sum_{i=1}^p \sum_{j=1}^p \frac{\tilde{b}_i \tilde{b}_j x_i x_j E_{ij}(T)}{\sum_{i=1}^p x_i \tilde{b}_i} Q'(\eta) \quad (5)$$

with

$$Q'(\eta) = \frac{\eta}{1 + \gamma \eta}$$

$E_{ij}$  denotes the binary energy parameter and varies with temperature according to

$$E_{ij} = E_{ij}^o \left( \frac{T^o}{T} \right)^r \quad T^o = 298.15 \text{ K} \quad (6)$$

$E_{ij}^o$  and  $r$  are two parameters adjusted using vapor-liquid equilibrium data. The isothermal VLE values between 243 K and 473 K and isobaric VLE values at atmospheric pressure reported in the literature and given in Table 5 were selected for this evaluation. We find  $E_{ij}^o = 365.8 \text{ J cm}^{-3}$  and  $r = -1.823$ . It should be noted that we have not taken into account our measurements in adjustment.

The relative mean deviation in the bubble-point pressure and absolute mean deviation in the vapor-phase composi-

**Table 1.** P,  $\rho$  Data for Methanol (1) + Water (2) at Different Temperatures

P/MPa	$\rho/\text{mol L}^{-1}$	T = 272.46 K																
17.355	52.3000	40.145	51.4514	37.121	49.0102	40.523	47.5560	29.198	45.6890	37.837	45.0270	28.986	43.4205	28.519	42.3008	28.519	T = 443.49 K	
15.863	52.2032	38.746	51.3544	35.653	48.9295	39.104	47.4764	27.703	45.6076	36.356	44.9517	27.598	43.3495	27.081	42.2324	27.081	T = 443.49 K	
14.346	52.1246	37.269	51.2799	34.171	48.8406	37.538	47.3855	26.201	45.5273	34.853	44.8806	26.151	43.2738	25.627	42.1678	25.627	T = 443.49 K	
12.905	52.0356	35.815	51.1904	32.735	48.7498	36.052	47.3090	24.723	45.4574	33.334	44.8032	24.659	43.1963	24.152	42.0993	24.152	T = 443.49 K	
11.482	51.9425	34.348	51.1072	31.233	48.6613	34.548	47.2250	23.272	45.3919	31.826	44.7247	23.158	43.1320	22.701	42.0337	22.701	T = 443.49 K	
9.949	51.8667	32.827	51.0249	29.745	48.5769	33.049	47.1382	21.813	45.3292	30.333	44.6445	21.773	43.0586	21.293	41.9751	21.293	T = 443.49 K	
8.476	51.7925	31.337	50.9375	28.268	48.4973	31.565	47.0473	20.441	45.2438	28.905	44.5616	20.368	42.9806	19.888	41.9182	19.888	T = 443.49 K	
7.021	51.7151	29.847	50.8400	26.757	48.4252	30.025	46.9689	19.079	45.1697	27.494	44.4835	18.902	42.9089	18.358	41.8444	18.358	T = 443.49 K	
5.601	51.6315	28.391	50.7448	25.266	48.3427	28.509	46.8831	17.598	45.0952	26.122	44.4024	17.362	42.8359	16.884	41.7733	16.884	T = 443.49 K	
4.077	51.5441	27.043	50.6649	23.902	48.2615	26.997	46.8021	16.131	45.0165	24.694	44.3273	15.842	42.7695	15.381	41.7031	15.381	T = 443.49 K	
2.596	51.4678	25.511	50.5900	22.435	48.1765	25.534	46.7254	14.686	44.9455	23.183	44.2589	14.343	42.7096	13.944	41.6344	13.944	T = 443.49 K	
1.128	51.3988	24.029	50.4983	21.009	48.0871	24.059	46.6468	13.375	44.8743	21.774	44.1626	12.937	42.6513	12.494	41.5766	12.494	T = 443.49 K	
		22.501	50.4026	19.506	48.0048	22.661	46.5739	12.005	44.8016	20.292	44.0865	11.401	42.5866	10.993	41.5127	10.993	T = 443.49 K	
		21.009	50.3123	18.055	47.9235	21.240	46.4950	10.641	44.7327	18.907	44.0191	9.926	42.5177	9.516	41.4552	9.516	T = 443.49 K	
		19.582	50.2236	16.588	47.8504	19.719	46.4122	9.334	44.6556	17.554	43.9426	8.423	42.4626	8.053	41.3906	8.053	T = 443.49 K	
		18.119	50.1485	15.230	47.7787	18.374	46.3355	7.894	44.5886	16.051	43.8673	6.935	42.3993	6.658	41.3371	6.658	T = 443.49 K	
		16.682	50.0708	13.751	47.7000	16.893	46.2692	6.492	44.5250	14.628	43.8131	5.566	42.3370	5.274	41.2804	5.274	T = 443.49 K	
		15.302	49.9821	12.323	47.6207	15.416	46.1876	5.141	44.4570	13.188	43.7382	4.134	42.2759	3.864	41.2186	3.864	T = 443.49 K	
		13.828	49.8892	10.931	47.5385	13.928	46.1188	3.816	44.4005	11.904	43.6678	2.747	42.2175	2.473	41.1474	2.473	T = 443.49 K	
		12.311	49.7985	9.598	47.4634	12.396	46.0542	2.519	44.3280	10.585	43.5991	1.199	40.9851	1.342	37.9460	1.342	T = 443.49 K	
		10.808	49.7160	8.113	47.3957	11.049	45.9800	1.255	44.2651	9.110	43.5257	0.784	37.1590	1.193	33.4167	1.193	T = 443.49 K	
		9.367	49.6361	6.712	47.3218	9.695	45.9021	0.464	41.6114	7.730	43.4633	0.732	33.7583	1.166	29.6370	1.166	T = 443.49 K	
		7.985	49.5624	5.269	47.2477	8.275	45.8338	0.423	39.7382	6.379	43.3917	0.708	29.9020	1.177	26.7206	1.177	T = 443.49 K	
		6.648	49.4886	3.889	47.1728	6.817	45.7665	0.318	33.8429	5.082	43.3240	0.679	26.9269	1.173	24.4234	1.173	T = 443.49 K	
		5.206	49.4055	2.564	47.1052	5.382	45.6896	0.287	29.9431	3.734	43.2380	0.681	24.5923	1.159	22.5790	1.159	T = 443.49 K	
		3.777	49.3208	1.206	47.0266	3.994	45.6208	0.255	26.9359	2.416	43.0233	0.669	22.7125	1.155	21.0424	1.155	T = 443.49 K	
		2.456	49.2504	1.087	49.1642	2.456	45.5423	0.239	24.5851	1.123	43.1462	0.646	21.1582	1.111	19.7261	1.111	T = 443.49 K	
						1.172	45.4777	0.228	22.6978	0.640	37.9061	0.660	19.8057	1.132	18.5419	1.132	T = 443.49 K	
						0.303	44.0635	0.243	20.8539	0.548	33.5597	0.682	18.6035	1.140	17.4350	1.140	T = 443.49 K	
						0.254	41.0485	0.238	19.5241	0.463	29.7931	0.624	17.4884	1.105	16.3584	1.105	T = 443.49 K	
						0.211	35.4289	0.230	18.3388	0.495	26.8609	0.654	16.4035	1.123	15.2750	1.123	T = 443.49 K	
						0.166	31.1505	0.215	17.2448	0.475	24.5511	0.655	15.3170	1.092	14.1606	1.092	T = 443.49 K	
						0.183	27.8672	0.231	16.1348	0.473	22.6819	0.648	14.2039	1.077	13.0241	1.077	T = 443.49 K	
						0.150	24.8712	0.224	15.0163	0.449	21.1392	0.619	13.0596	1.059	12.9064	1.059	T = 443.49 K	
						0.159	22.8799	0.210	13.8605	0.437	19.8100	0.420	18.6181	0.420	17.5121	0.420	T = 443.49 K	
						0.153	21.2366	0.208	12.6830	0.400	12.6830	0.400	11.4040	0.400	10.397	0.400	T = 443.49 K	
						0.191	19.8334	0.191	18.6029	0.397	18.6029	0.397	17.5121	0.397	16.4346	0.397	T = 443.49 K	
						0.104	18.6029	0.104	17.4066	0.397	17.4066	0.397	16.3565	0.397	15.2456	0.397	T = 443.49 K	
						0.125	17.4196	0.125	16.2233	0.397	16.2233	0.397	15.1606	0.397	14.0730	0.397	T = 443.49 K	
						0.108	16.2964	0.108	15.1308	0.397	15.1308	0.397	14.0730	0.397	13.0241	0.397	T = 443.49 K	

**Table 1. (Continued)**

P/MPa	$\rho/\text{mol L}^{-1}$	P/MPa	$\rho/\text{mol L}^{-1}$										
15.193	41.8476	27.442	40.9851	31.872	39.7126	38.941	38.6364	36.860	37.8328	38.835	36.8795	38.419	36.2004
13.663	41.7896	25.976	40.9228	30.436	39.6629	37.551	38.5856	35.373	37.7823	37.246	36.8265	36.823	36.1508
12.207	41.7327	24.619	40.8068	28.952	39.6132	36.164	38.5290	33.772	37.7319	35.664	36.7963	35.212	36.1110
10.736	41.6688	23.118	40.7473	27.478	39.5625	34.761	38.4712	32.210	37.6796	34.123	36.7462	33.609	36.0757
9.232	41.6102	21.641	40.6929	25.986	39.5102	33.435	38.4215	30.636	37.6331	32.554	36.7034	32.019	36.0286
7.776	41.5529	20.121	40.6256	24.518	39.4609	31.933	38.3749	29.062	37.5788	30.951	36.6643	30.406	35.9888
6.350	41.4966	18.689	40.5881	30.452	39.4100	30.452	38.3311	27.468	37.5256	29.436	36.8235	28.805	35.9424
4.877	41.4289	17.284	40.5305	21.648	39.3636	28.981	38.2849	25.944	37.4716	27.968	36.5798	27.217	35.8932
3.501	41.3884	15.853	40.4741	20.242	39.3116	27.511	38.2394	24.415	37.4260	26.401	36.5359	25.605	35.8433
2.114	41.3293	14.387	40.4233	18.773	39.2623	26.026	38.1928	22.937	37.3874	24.862	36.4869	24.002	35.7974
1.115	41.2802	12.993	40.3807	17.287	39.2118	24.557	38.1450	21.403	37.3406	23.313	36.4415	22.403	35.7543
		11.602	40.3375	15.876	39.1645	23.080	38.0994	19.944	37.3733	21.733	36.3995	20.810	35.7019
		10.186	40.2843	14.445	39.1123	21.579	38.0555	18.401	37.2379	20.168	36.3530	19.214	35.6547
		8.730	40.2241	12.981	39.0618	20.062	38.0077	16.837	37.1910	18.672	36.3089	17.606	35.6125
		7.306	40.1691	11.503	39.0143	18.572	37.9618	15.301	37.0887	17.069	36.2677	15.986	35.5683
		5.817	40.1209	10.080	38.9554	17.129	37.9168	13.797	37.0395	15.488	36.2242	14.419	35.5270
		4.411	40.0702	8.579	38.9161	15.667	37.8690	12.315	36.9894	14.001	36.1851	12.821	35.4842
		3.031	40.0114	7.110	38.8687	14.255	37.8268	10.841	36.9470	12.426	36.1407	11.216	35.4378
		1.631	39.9581	5.148	38.8174	12.809	37.7829	9.357	36.8991	10.939	36.0951	9.659	35.3952
		1.158	39.9016	3.725	38.7673	11.388	37.7334	7.868	36.8575	9.430	36.0527	8.010	35.3557
				2.397	38.7103	9.931	37.6873	6.365	36.8125	7.906	36.0172	6.414	35.3147
				1.150	38.6650	8.531	37.6405	4.882	36.7663	6.302	35.9786	4.824	34.3444
						7.067	37.5976	3.432	36.7163	4.789	35.9312	3.365	35.2096
						5.589	37.5569	2.078	36.6552	3.401	35.8883	2.307	35.1677
						4.137	37.5064	0.990	33.9100	2.108	35.8345	1.107	32.8230
						2.674	37.4597	0.395	30.4580	0.937	33.2874	1.009	29.5311
						1.312	37.4068	0.389	27.6454	0.713	29.3836	0.977	26.9424
						0.925	37.3046	0.322	25.4014	0.627	27.1880	0.961	24.8622
						0.635	33.4597	0.287	23.5835	0.590	25.0391	0.916	23.1514
						0.485	32.8399	0.233	22.0486	0.549	23.2849	0.937	21.6925
						0.259	29.5600	0.287	20.7117	0.588	21.7973	0.873	20.4005
						0.182	26.9367	0.225	19.4903	0.564	20.2565	0.900	19.2097
						0.129	24.8407	0.253	18.3268	0.548	19.0668	0.883	18.0584
						0.151	23.1167	0.254	17.1747	0.538	17.9135	0.845	16.9016
						0.125	21.6509	0.253	16.0046	0.494	16.7597	0.852	15.7255
						0.139	20.1183	0.240	14.7970	0.518	15.5809	0.855	14.5181
										0.501		14.3665	

$T = 302.32 \text{ K}$        $x_1 = 0.2872$        $T = 363.00 \text{ K}$        $x_1 = 0.2872$        $T = 383.52 \text{ K}$        $x_1 = 0.2872$        $T = 403.52 \text{ K}$        $x_1 = 0.2872$   
 $T = 424.29 \text{ K}$        $x_1 = 0.2872$        $T = 442.71 \text{ K}$        $x_1 = 0.2872$        $T = 462.71 \text{ K}$        $x_1 = 0.2872$        $T = 482.71 \text{ K}$        $x_1 = 0.2872$

$T = 424.29 \text{ K}$        $x_1 = 0.2872$        $T = 442.71 \text{ K}$        $x_1 = 0.2872$        $T = 462.71 \text{ K}$        $x_1 = 0.2872$        $T = 482.71 \text{ K}$        $x_1 = 0.2872$

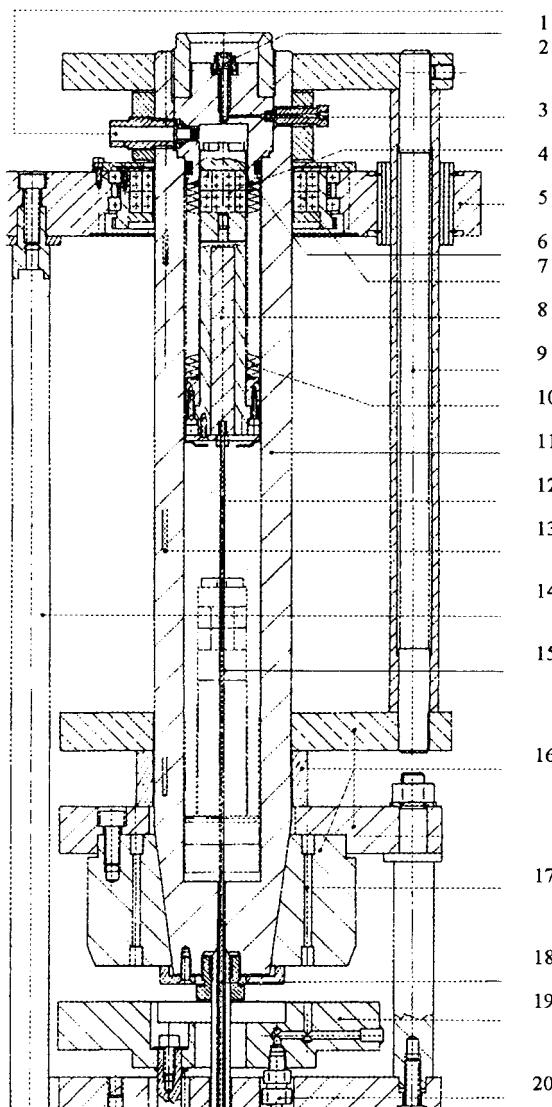
**Table 1. (Continued)**

P/MPa	$\rho/\text{mol L}^{-1}$	P/MPa	$\rho/\text{mol L}^{-1}$	P/MPa	$\rho/\text{mol L}^{-1}$	P/MPa	$\rho/\text{mol L}^{-1}$	P/MPa	$\rho/\text{mol L}^{-1}$	P/MPa	$\rho/\text{mol L}^{-1}$	P/MPa	$\rho/\text{mol L}^{-1}$	P/MPa	$\rho/\text{mol L}^{-1}$
T = 256.87 K	T = 272.39 K	T = 301.67 K	T = 332.82 K	T = 363.14 K	T = 383.25 K	T = 403.64 K	T = 424.34 K	T = 442.72 K	T = 462.72 K	T = 482.72 K	T = 502.72 K	T = 522.72 K	T = 542.72 K	T = 562.72 K	T = 582.72 K
14.026 38.8674	18.459 38.0520	39.013 37.1646	34.153 35.1638	39.095 33.8206	38.128 32.5884	38.223 31.6585	34.959 30.6603	14.043 28.9217	14.043 28.9217	14.043 28.9217	14.043 28.9217	14.043 28.9217	14.043 28.9217	14.043 28.9217	14.043 28.9217
12.519 38.7965	16.955 37.9798	37.625 37.0993	32.695 35.1029	37.716 33.7629	36.775 32.5371	36.859 31.6046	33.676 30.6126	9.146 28.7329	9.146 28.7329	9.146 28.7329	9.146 28.7329	9.146 28.7329	9.146 28.7329	9.146 28.7329	9.146 28.7329
11.059 38.7274	15.423 37.9116	36.151 37.0413	31.197 35.0458	36.315 33.7024	35.372 32.4856	35.446 31.5514	32.417 30.5653	7.814 28.6879	7.814 28.6879	7.814 28.6879	7.814 28.6879	7.814 28.6879	7.814 28.6879	7.814 28.6879	7.814 28.6879
9.582 38.6638	13.925 37.8488	34.649 36.9643	29.694 34.9800	34.917 33.6408	33.985 32.4388	34.077 31.4995	31.136 30.5148	6.663 28.6384	6.663 28.6384	6.663 28.6384	6.663 28.6384	6.663 28.6384	6.663 28.6384	6.663 28.6384	6.663 28.6384
8.049 38.5902	12.457 36.9047	36.194 36.9047	28.240 34.9167	33.530 33.5839	32.661 32.3925	32.693 31.4456	29.839 30.4637	5.353 28.5922	5.353 28.5922	5.353 28.5922	5.353 28.5922	5.353 28.5922	5.353 28.5922	5.353 28.5922	5.353 28.5922
6.614 38.5192	11.021 37.7079	31.795 36.8453	26.762 34.8348	32.128 33.5263	31.280 32.3444	31.276 31.3930	28.581 30.4140	4.054 28.5470	4.054 28.5470	4.054 28.5470	4.054 28.5470	4.054 28.5470	4.054 28.5470	4.054 28.5470	4.054 28.5470
5.094 38.4752	9.587 37.6411	30.368 36.8067	25.249 34.7921	30.690 33.4685	29.922 32.2996	29.865 31.3590	27.277 30.3641	2.810 28.4974	2.810 28.4974	2.810 28.4974	2.810 28.4974	2.810 28.4974	2.810 28.4974	2.810 28.4974	2.810 28.4974
3.734 38.3995	8.125 37.5677	28.836 36.7557	23.743 34.7344	29.326 33.4090	28.520 32.2492	28.491 31.2906	26.018 30.3176	2.142 26.8161	2.142 26.8161	2.142 26.8161	2.142 26.8161	2.142 26.8161	2.142 26.8161	2.142 26.8161	2.142 26.8161
2.217 38.2449	6.683 37.4999	27.372 36.7045	22.246 34.6789	27.952 33.3488	27.185 32.2003	27.129 31.2383	24.723 30.2884	1.881 24.4609	1.881 24.4609	1.881 24.4609	1.881 24.4609	1.881 24.4609	1.881 24.4609	1.881 24.4609	1.881 24.4609
5.230 37.4279	25.940 36.5701	20.765 34.6192	16.520 32.9282	26.551 33.2928	25.807 32.1531	25.673 31.1875	23.477 30.2229	1.753 21.3522	1.753 21.3522	1.753 21.3522	1.753 21.3522	1.753 21.3522	1.753 21.3522	1.753 21.3522	1.753 21.3522
3.799 37.3662	24.454 36.5134	19.261 34.5536	15.172 32.2357	25.172 33.1762	23.1049 32.0569	24.272 31.1406	22.192 30.1745	1.702 18.9326	1.702 18.9326	1.702 18.9326	1.702 18.9326	1.702 18.9326	1.702 18.9326	1.702 18.9326	1.702 18.9326
2.366 37.2980	22.986 36.4423	17.796 34.4855	13.1762 33.1767	23.767 33.1762	23.019 32.0569	22.894 31.0892	20.918 30.1301	1.674 17.1491	1.674 17.1491	1.674 17.1491	1.674 17.1491	1.674 17.1491	1.674 17.1491	1.674 17.1491	1.674 17.1491
21.556 36.3696	16.317 36.4238	22.411 34.3612	21.112 33.0627	21.665 33.0105	21.487 32.0105	21.487 31.0378	19.650 30.0815	1.643 15.7025	1.643 15.7025	1.643 15.7025	1.643 15.7025	1.643 15.7025	1.643 15.7025	1.643 15.7025	1.643 15.7025
20.104 36.2855	14.816 36.2285	13.319 36.2294	13.319 34.3004	20.300 33.0070	20.040 31.9614	20.040 30.9907	18.350 30.0307	1.637 14.5364	1.637 14.5364	1.637 14.5364	1.637 14.5364	1.637 14.5364	1.637 14.5364	1.637 14.5364	1.637 14.5364
18.625 36.1654	11.896 34.2366	17.122 34.1786	10.331 34.1786	16.926 32.8973	16.133 32.8973	16.743 31.8421	15.743 30.8421	1.622 13.5681	1.622 13.5681	1.622 13.5681	1.622 13.5681	1.622 13.5681	1.622 13.5681	1.622 13.5681	1.622 13.5681
15.669 36.0869	8.799 36.0219	14.199 36.0219	8.799 34.1233	15.339 32.8355	14.727 32.8355	14.332 31.7921	13.321 30.8447	1.608 11.2704	1.608 11.2704	1.608 11.2704	1.608 11.2704	1.608 11.2704	1.608 11.2704	1.608 11.2704	1.608 11.2704
12.775 35.9419	7.297 35.7297	13.070 34.0701	14.148 32.7732	13.349 32.7732	13.791 32.7221	11.990 31.6823	12.896 30.7464	1.592 10.5835	1.592 10.5835	1.592 10.5835	1.592 10.5835	1.592 10.5835	1.592 10.5835	1.592 10.5835	1.592 10.5835
11.321 35.8645	5.808 34.0100	12.838 34.0100	12.838 34.0100	13.000 32.6656	10.587 32.6656	10.142 31.6366	10.142 30.6988	1.565 9.8893	1.565 9.8893	1.565 9.8893	1.565 9.8893	1.565 9.8893	1.565 9.8893	1.565 9.8893	1.565 9.8893
9.842 35.7936	4.245 33.9449	8.386 33.9449	10.443 33.9449	10.024 32.6064	9.293 32.6064	9.581 31.5891	8.892 30.5996	1.595 9.1787	1.595 9.1787	1.595 9.1787	1.595 9.1787	1.595 9.1787	1.595 9.1787	1.595 9.1787	1.595 9.1787
8.386 35.7277	2.867 33.8872	8.678 33.8872	8.678 33.8872	7.973 32.5502	7.973 31.5480	7.563 31.5480	7.033 30.5532	1.584 8.3584	1.584 8.3584	1.584 8.3584	1.584 8.3584	1.584 8.3584	1.584 8.3584	1.584 8.3584	1.584 8.3584
6.885 35.6605	5.605 35.6225	7.508 35.6225	6.703 34.4926	6.703 34.4926	5.330 32.4436	5.330 31.4568	4.938 30.4598	5.741 29.5695	5.741 29.5695	5.741 29.5695	5.741 29.5695	5.741 29.5695	5.741 29.5695	5.741 29.5695	5.741 29.5695
4.037 35.5847	4.037 35.4797	6.199 4.037 35.4797	4.759 32.3907	4.047 32.3907	31.4144 31.4144	3.617 31.4144	3.617 30.4128	4.497 30.4823	4.497 30.4823	4.497 30.4823	4.497 30.4823	4.497 30.4823	4.497 30.4823	4.497 30.4823	4.497 30.4823
2.746 35.4797			3.493 32.3407	3.224 32.2892	2.771 32.2892	2.286 31.3662	2.286 30.3887	3.197 29.4846							
			2.224 32.2892	1.617 32.2892	1.617 30.9101	1.348 29.3962	1.119 29.3962								
			1.033 31.5473	1.017 31.5473	0.705 29.9495	0.668 29.9495	0.668 28.2593	1.065 17.5204							
			0.365 25.6849	0.568 25.6849	0.530 25.5891	0.530 25.5891	0.530 24.1331	1.041 15.9810							
			0.234 22.3322	0.436 22.3322	0.436 22.1267	0.692 22.1267	0.692 21.0064	1.012 14.7572							
			0.212 19.6228	0.378 19.6228	0.378 19.4623	0.648 19.4623	0.648 18.6451	1.021 13.7428							
			0.211 17.5868	0.346 17.5868	0.346 17.4660	0.652 17.4660	0.652 16.5538	0.999 12.7321							
			0.162 16.0050	0.305 16.0050	0.305 15.9236	0.578 15.9236	0.578 15.2078	0.975 11.9734							
			0.109 14.7545	0.319 14.7545	0.319 14.7024	0.598 14.7024	0.598 14.1196	0.983 11.2631							
			0.149 13.7332	0.278 13.7332	0.278 13.6966	0.550 13.6966	0.550 13.2013	0.981 10.5754							
			0.119 12.7010	0.260 12.7010	0.260 12.8332	0.575 12.8332	0.575 12.3966	0.948 9.8790							
			0.105 11.9298	0.289 11.9298	0.289 11.9230	0.555 11.9230	0.555 11.6613	0.961 9.1610							
			0.122 11.2172	0.278 11.2172	0.278 11.2126	0.537 11.2126	0.537 10.9647	0.948 8.4296							
			0.107 10.5236	0.276 10.5236	0.276 10.5181	0.551 10.5181	0.551 10.2772								
			0.109 9.6868	0.273 9.6868	0.273 9.8173	0.550 9.8173	0.550 9.4003	0.550 8.6698							
			0.104 8.9597	0.265 8.9597	0.265 8.9095	0.544 8.9095	0.544 8.3612	0.544 8.2197							

Table 1. (Continued)

$P/\text{MPa}$	$\rho/\text{mol L}^{-1}$														
T = 257.34 K		T = 272.91 K		T = 302.47 K		T = 333.14 K		T = 363.05 K		T = 383.29 K		T = 403.43 K		T = 423.26 K	
15.762	34.9700	28.559	34.6884	36.268	33.4872	39.659	31.9314	38.622	30.3356	36.281	29.3854	38.996	28.6290	38.939	27.8557
14.417	34.9069	27.219	34.6306	34.907	33.4294	38.252	31.8773	37.091	30.2882	34.687	29.3492	37.547	28.5867	37.353	27.8074
13.118	34.8471	25.854	34.5698	33.593	33.3669	36.757	31.8177	35.568	30.2390	33.122	29.3013	36.080	28.5412	35.776	27.7642
11.826	34.7852	24.543	34.5092	32.283	33.3053	35.269	31.7535	34.088	30.1881	31.640	29.2520	34.571	28.4934	34.173	27.7152
10.515	34.7190	23.253	34.4429	30.958	33.2474	32.704	31.7035	32.581	30.1389	30.118	29.2074	33.050	28.4487	32.553	27.6717
9.211	34.6582	21.892	34.3839	29.635	33.1942	32.254	31.6484	31.112	30.0879	28.617	29.1648	31.559	28.4057	30.940	26.8213
7.943	34.5966	20.567	34.3286	28.328	33.1366	30.781	31.5889	29.582	30.0389	27.127	29.1216	30.028	28.3661	29.356	27.5758
6.622	34.5326	19.212	34.2658	26.963	33.0795	29.367	31.5384	28.035	29.9948	25.605	29.0790	28.553	28.3236	27.734	27.5290
5.372	34.4651	17.910	34.2054	25.641	33.0214	27.898	31.4810	26.534	29.9406	24.110	29.0346	27.063	28.2795	26.093	27.4865
4.032	34.4099	16.576	34.1419	24.321	32.9588	26.367	31.4269	25.070	29.9012	22.607	28.9929	25.549	28.2367	24.482	27.4429
2.698	34.3496	15.199	34.0815	22.980	32.9045	24.901	31.3748	23.531	29.8579	21.119	28.9521	24.027	28.1954	22.858	27.3964
1.457	34.3007	13.902	34.0206	21.616	32.8490	23.377	31.3181	22.020	29.8041	20.632	28.9112	22.553	28.1488	21.260	27.3533
		12.591	33.9614	20.312	32.7913	21.887	31.2642	20.549	29.7551	18.120	28.8646	20.989	28.1030	19.655	27.3067
		11.288	33.8974	18.980	32.7318	20.422	31.2054	19.063	29.7163	16.606	28.8186	19.468	28.0586	18.061	27.2657
		9.820	33.8389	17.620	32.6751	18.889	31.1443	17.560	29.6744	15.086	28.7718	17.965	28.0181	16.494	27.2236
		8.466	33.7841	16.314	32.6145	17.391	31.0856	16.065	29.6319	13.563	28.7262	16.526	27.9768	14.871	27.1775
		7.141	33.7242	14.990	32.5550	15.913	31.0288	14.526	29.5935	12.029	28.6840	15.019	27.9363	13.240	27.1400
		5.905	33.6610	13.685	32.4997	14.426	30.9751	13.052	29.5498	10.526	28.6391	13.486	27.8929	11.654	27.1069
		4.550	33.5964	12.322	32.4429	13.020	30.9214	11.545	29.4992	9.045	28.5980	11.999	27.8531	9.975	27.0647
		3.264	33.5380	10.675	32.3860	11.593	30.8667	10.024	29.4792	7.513	28.5532	10.533	27.8110	8.345	27.0198
		1.900	33.4853	9.664	32.2734	10.137	30.8165	8.539	29.4088	5.985	28.5116	9.060	27.7720	6.834	26.9785
		1.172	33.4260	8.340	32.2255	8.540	30.7640	7.047	29.3696	4.459	28.4654	7.636	27.7270	5.295	26.9332
		7.015	32.1692	6.947	30.7079	5.537	29.3253	3.110	28.4174	6.040	27.6846	4.852	26.8956	1.876	16.9983
		5.637	32.1116	5.488	30.6633	4.345	29.2828	1.731	28.3720	4.584	27.6472	2.549	26.8507	1.913	15.5124
		4.316	32.0516	4.128	30.6115	2.634	29.2301	0.995	28.3509	3.104	27.6020	1.332	25.4545	1.855	14.3215
		2.938	32.0027	2.753	30.5616	1.197	29.1871	0.391	24.3320	1.772	27.5595	1.264	23.1957	1.869	21.3294
		1.688	31.9490	1.420	30.5212	1.061	29.1560	0.388	21.0257	0.942	27.5290	1.193	20.3163	1.879	13.3379
		0.180	13.4720	0.180	13.4720	0.347	11.7066	0.695	20.1435	1.183	18.1122	1.857	11.7535	1.145	12.4982
		0.225	19.6062	0.225	19.6062	0.380	15.4494	0.692	17.6431	1.203	15.0410	1.886	10.2655	1.166	8.9122
		0.255	17.2365	0.255	17.2365	0.369	14.2648	0.729	16.0273	1.188	13.9368	1.837	9.5975	1.145	8.2096
		0.209	15.7073	0.209	15.7073	0.381	13.2855	0.698	14.7389	1.147	13.0120	1.859	8.9122	1.145	7.8781
		0.206	14.4824	0.206	14.4824	0.392	12.4489	0.691	13.6819	1.192	12.2120	1.872	8.2096	1.145	7.7911
		0.162	10.4832	0.162	10.4832	0.288	8.9867	0.702	9.9676	1.45	9.2898	0.704	8.0775	0.669	8.5935
		0.140	9.8148	0.140	9.8148	0.219	8.2833	0.219	8.2833	0.219	8.2833	0.219	8.0775	0.602	7.8781

Table 1. (Continued)



**Figure 2.** Schematic diagram of the measurement cell: (1) saphir windows; (2) stainless steel valve; (3) fluid introduction; (4) internal iron kernel for the stirrer; (5) stirrer support; (6) stirrer; (7) external iron kernel for the stirrer; (8) copper cylinder; (9) copper column; (10) bellow; (11) chamber; (12) copper rod; (13) thermocouple; (14) column connecting the support of the external stirrer with the micrometric table; (15) low position of the stirrer; (16) copper mass for transferring the heating or cooling fluid to the bottom of the bellow; (17) cooling circuit; (18) entrance tube of the compression fluid; (19) cooling platform; (20) entrance of liquid nitrogen.

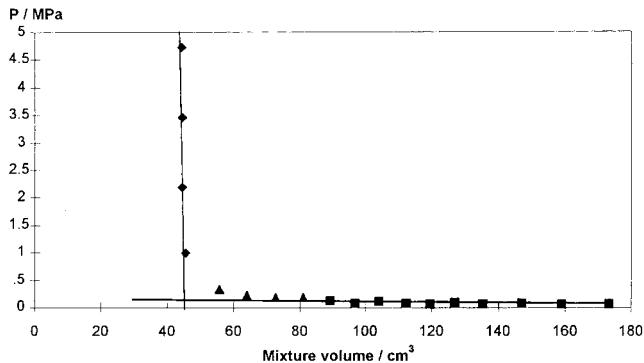
tion defined by

$$\Delta P/P(\%) = \frac{100}{N_P} \sum_{i=1}^{N_P} \left| \frac{P_{\text{exp},i} - P_{\text{cal},i}}{P_{\text{exp},i}} \right| \quad (7)$$

$$\Delta y = \frac{1}{N_y} \sum_{i=1}^{N_y} |y_{\text{exp},i} - y_{\text{cal},i}| \quad (8)$$

are given in Table 5 where  $N_P$  and  $N_y$  are respectively the numbers of determinations of bubble-point pressures and of vapor-phase compositions.

The vapor–liquid equilibrium of methanol + water has been measured by Griswold and Wong (1952) between 373.15 K and 523.15 K, by Schroder (1958) at 413.15 K, and by Hirata and Suda (1967) and Hirata et al. (1975)



**Figure 3.** Determination of bubble pressure of methanol (1) + water (2) at 363.15 K for  $x_1 = 0.4980$ : ◆, data in single-phase region (liquid); ■, data in two-phase region; ▲, data in two-phase region not taken into account in linear regression.

**Table 2. Bubble Pressures for the Methanol (1) + Water (2) System at Five Different Temperatures**

$x_1$	P/MPa				
	363.15 K	383.15 K	403.15 K	424.15 K	442.15 K
0.1061	0.117	0.227	0.403	0.665	1.157
0.2872	0.153	0.293	0.567	0.937	1.477
0.4980	0.181	0.369	0.647	1.073	1.704
0.6876	0.219	0.401	0.715	1.218	1.906
0.9061	0.238	0.458	0.844	1.296	2.093

**Table 3. Comparison of Experimental and Calculated Liquid-Phase Density Data at Selected Temperatures and Pressures**

$T/K$	pressure range (MPa)	no. of data	$\Delta\rho/\rho (\%)$	$\beta_r(\rho)$
332.55	13.751–1.150	44	2.63	-0.30
363.17	13.052–1.062	46	2.62	-1.17
383.57	13.039–0.995	46	2.89	-1.75
403.52	12.896–0.942	45	2.97	-1.96
424.05	12.937–2.126	40	2.85	-1.81
443.50	12.763–2.411	37	3.18	-1.76

**Table 4. Pure Component Parameters Used in This Study**

compd	$T_c/K$	$P_c/MPa$	$T_b/K$	$b/cm^3\text{mol}^{-1}$	$m_1$	$m_2$
methanol	512.58	8.094	337.70	23.995	1.080 64	-0.170 98
water	647.37	22.120	373.15	11.089	1.358 60	0.165 64

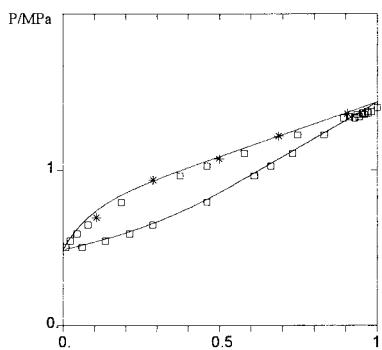
**Table 5. Vapor–Liquid Equilibrium Results for Methanol + Water**

type	ref	temp range (K)	pressure range (MPa)	N <sub>P</sub> ΔP/P (%) N <sub>y</sub> Δy			
				N <sub>P</sub>	ΔP/P (%)	N <sub>y</sub>	Δy
isothermal	1 to 13	243–474	0.00005–3.950	449	1.86	262	0.018
isobaric	14 to 39	307–421	0.026–0.507	422	2.13	387	0.011
global				871	1.99	649	0.014

at pressures of 0.3 MPa and 0.5 MPa. The results obtained from these authors and our data are summarized in Table 6. The agreement is satisfactory. Moreover, we can remark in Figure 4 that our own measurements at 424.15 K agree with those of Griswold and Wong (1952) at 423.15 K, the only reference temperature.

## Conclusion

We have described a high-pressure apparatus designed to obtain pressure–density–temperature data of a pure-component or a mixture over the temperature range 210 K–470 K and at pressures up to 70 MPa. The densities of



**Figure 4.** Vapor–liquid equilibria of the methanol–water binary system at 424.15 K. Calculated curve: full line. Data: \*, our work; □, Griswold and Wong at 423.15 K.

**Table 6. Relative Mean Deviations in the Bubble-Point Pressure for Our Data and Those Reported in the Literature**

T/K	P/MPa	N <sub>p</sub>	ΔP/P (%)	ref
363.15		5	1.76	our work
383.15		5	1.33	our work
403.15		5	2.79	our work
424.15		5	2.67	our work
442.15		5	1.10	our work
373.15	18		1.54	Griswold and Wong
423.15	16		0.81	Griswold and Wong
473.15	17		3.82	Griswold and Wong
413.15	6		1.29	Schroeder
0.304	10		2.96	Hirata and Suda
0.507	11		2.14	Hirata and Suda
0.304	26		1.78	Hirata et al.
0.507	26		2.21	Hirata et al.

the methanol + water have been measured in the single-phase and two-phase region. The VLE pressure–composition data obtained from densities are in good agreement with literature values that have been fitted to the excess function-equation of state model by adjusting an interaction parameter.

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